



Dept. of Electrical Engineering  
First Exam, Summer Semester: 2014/2015

Course Title: Instrumentation and Measurement	Date: 10/8/2015
Course No: (610332)	Time Allowed: 50 Minutes
Lecturer: Dr. Mohammad Abu-Naser	No. of Pages: 1

**Question 1:** (6Mark)

Objectives: This question is related to statistical analysis

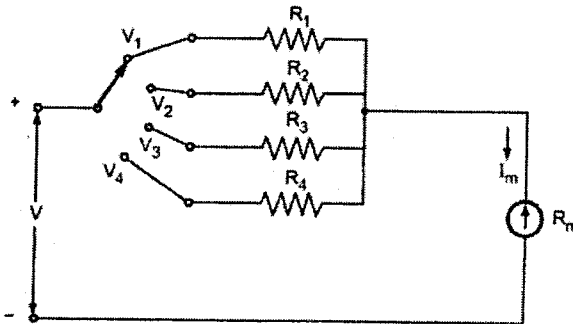
- 1) Define the terms (a) accuracy (b) precision.
- 2) Five voltage measurements were 10.1V, 10.5V, 9.6V, 9.8V, 10V. Assume only random errors are present. Calculate:
  - (a) Arithmetic mean.
  - (b) Standard deviation.
  - (c) Variance.
  - (d) Probable error.

**Question 2:** (7Mark)

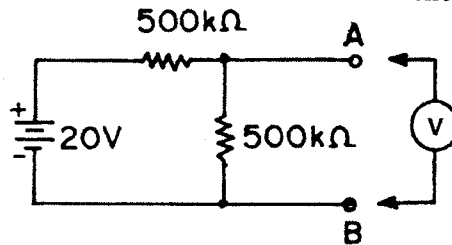
Objectives: This question is related to galvanometer

A basic D'Arsonval movement with a full scale deflection current of  $50 \mu\text{A}$  and an internal resistance of  $1800 \Omega$  is to be converted into a 0-1 V, 0-5 V, 0-25 V, and 0-125 V multi-range voltmeter using individual multipliers for each range.

- (a) Calculate the individual multipliers  $R_1, R_2, R_3,$  and  $R_4$ .



- (b) Calculate the sensitivity of the voltmeter.  
 (c) What would the voltmeter read on the 25 V range if connected across the  $500 \text{ k}\Omega$  resistor between terminals A and B shown in the following figure.



**Question 3:** (7Mark)

Objectives: This question is related to electrodynamicometer

- 1) Prove that the average deflection of electrodynamicometer type wattmeter is proportional to  $V I \cos \phi$ .
- 2) Explain the advantages and disadvantages of electrodynamicometer type instruments.

# Instrumentation and Measurement

First Exam  
Summer Semester 2014/2015

## Question 1

1) Accuracy: the degree of closeness of a measured value compared to the true value.

Precision: a measure of repeatability of measurements i.e., successive readings do not differ

$$2) \bar{V} = \frac{1}{5} \sum_{i=1}^5 V_i$$

$$= \frac{1}{5} \times 50 = 10 \text{ V}$$

$$\sigma = \sqrt{\frac{1}{4} \sum_{i=1}^5 d_i^2}$$

$$= \sqrt{\frac{1}{4} \times 0.46} = 0.3391 \text{ V}$$

V	d	d <sup>2</sup>
10.1	0.1	0.01
10.5	0.5	0.25
9.6	-0.4	0.16
9.8	-0.2	0.04
10	0	0
$\Sigma V = 50$		0.46

$$\sigma^2 = (0.3391)^2 = 0.115 \text{ V}^2$$

$$r = 0.6745 \sigma = 0.6745 \times 0.3391 = 0.2287 \text{ V}$$

## Question 2

$$a) \frac{I = V_{\text{range}}}{R_1 = \frac{V_1}{I_{fd}}} = \frac{1}{50 \times 10^{-6}} = 20 \text{ k}\Omega$$

$$\rightarrow R_1 - R_1 - R_m = 20 \text{ k}\Omega - 1.8 \text{ k}\Omega = 18.2 \text{ k}\Omega$$

5-V range

$$R_1 = \frac{V_2}{I_{fd}} = \frac{5}{50 \times 10^{-6}} = 100 \text{ k}\Omega$$

$$\rightarrow R_2 - R_1 - R_m = 100 \text{ k}\Omega - 1.8 \text{ k}\Omega = 98.2 \text{ k}\Omega$$

25-V range

$$R_T = \frac{V_3}{I_{fsd}} = \frac{25}{50 \times 10^{-6}} = 500 \text{ k}\Omega$$

$$\rightarrow R_2 = R_T = R_{in} = 500 \text{ k}\Omega + 18 \text{ k}\Omega = 498.2 \text{ k}\Omega$$

125-V range

$$R_T = \frac{V_4}{I_{fsd}} = \frac{125}{50 \times 10^{-6}} = 2500 \text{ k}\Omega$$

$$\rightarrow R_4 = R_T = R_{in} = 2500 \text{ k}\Omega + 18 \text{ k}\Omega = 2498.2 \text{ k}\Omega$$

$$b) S = \frac{1}{I_{fsd}} = \frac{1}{50 \times 10^{-6}} = 20 \text{ k}\Omega/\text{V}$$

$$c) R_V = S \times V_{\text{range}} \\ = 20 \text{ k}\Omega/\text{V} \times 25 \text{ V} = 500 \text{ k}\Omega$$

$$R_p = 500 \text{ k}\Omega \parallel R_V = 500 \text{ k}\Omega \parallel 500 \text{ k}\Omega = 250 \text{ k}\Omega$$

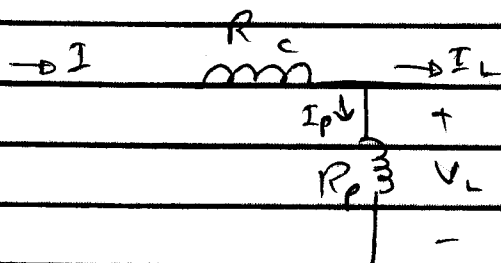
$$V_{\text{voltage}} = 20 \text{ V} \times \frac{250 \text{ k}\Omega}{750 \text{ k}\Omega} = 6.67 \text{ V}$$

Question 3

- 1)  $T \propto \beta A I_N$   
but  $\beta \propto I_p$   
and  $I = I_L + I_p \approx I_L$   
 $\Rightarrow T \propto I_p I_L$  (AN)

$$\text{since } I_p = \frac{V_L}{R_p}$$

$$\Rightarrow T \propto V_L I_L$$



So due to inertia of moving coil

$$\text{Deflection} \propto \frac{1}{T} \int_0^T V_c I_c dt$$

$$\text{let } V_c = V_m \sin(\omega t)$$

$$\text{and } I_c = I_m \sin(\omega t - \phi)$$

$$\begin{aligned} V_c(t) I_c(t) &= V_m I_m \sin \omega t \sin(\omega t - \phi) \\ &= \frac{1}{2} V_m I_m [\cos \phi - \cos(2\omega t - \phi)] \\ &= \frac{V I}{2} [\cos \phi - \cos(2\omega t - \phi)] \end{aligned}$$

Hence

$$\text{Deflection} \propto \frac{1}{T} \int_0^T V I [\cos \phi - \underbrace{\cos(2\omega t - \phi)}_{\text{periodic} \rightarrow \text{average is zero}}] dt$$

$$\text{Deflection} \propto \frac{V I}{T} \int_0^T \cos \phi dt$$

$$\text{Deflection} \propto V I \cos \phi$$

Advantages:

- 1) high accuracy
- 2) used for both AC and DC
- 3) accurate RMS value irrespective of waveform

Disadvantages:

- 1) high power consumption since it needs to supply its own magnetic flux
- 2) low sensitivity compared to PMMC, so it has high loading effect
- 3) expensive